Advanced Statistics, 2022

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Problem Set 2. Probability theory - counting, conditional probability, independence

References

- FPP: Statistics (4/e), Freedman, Pisani, Purves
- Wasserman: All of Statistics, Springer, 2003
- JWHT: An Introduction to Statistical Learning with Applications in R, James, Witten, Hastie and Tibshirani, Springer, 2017
- VS: An Introduction to R, Venables and Smith
- **1.** FPP page 227: Exercise set B
- 2. FPP page 230: Exercise set C
- **3.** FPP page 230: Exercise set D
- **4.** FPP page 235: 3, 5, 6, 7, 8, 9, 10
- **5.** FPP pages 240-2411: 1, 2, 3, 4
- 6. FPP pages 242-243: Exercise set B
- **7.** FPP pages 246-247: Exercise set C
- 8. FPP pages 250-251: Exercise set D
- **9.** FPP pages 252-254: 1, 3, 4, 5, 7, 8, 10, 12

10. Describe the Paradox of Chevalier de Méré. Resolve the paradox.

11. In how many ways can eight colored beads, all colored differently, be arranged on (i) a straight wire and (ii) a circular necklace?

12. A firm has to choose seven people from its R&D team of eleven to send to a conference on computer systems. How many ways are there of doing this

- i. when there are no restrictions?
- ii. when two of the team are so indispensable that only one of them can be permitted to go?
- iii. when it is essential that a certain member of the team goes?

13. Prove that the number of ways that a group of r objects can be chosen from n objects using sampling with replacement where the order of selection does not matter is given by $\binom{n+r-1}{r}$.

14. State and prove inclusion-exclusion principle.